Using data corresponding to 6.0 fb$^{-1}$ of $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV collected by the CDF II detector, we present a cross section measurement of top-quark pair production with an additional radiated photon, $t\gamma$. The events are selected by looking for a lepton ($l$), a photon ($\gamma$), significant transverse momentum imbalance ($E_T$), large total transverse energy, and three or more jets, with at least one identified as containing a $b$ quark ($b$). The $t\gamma$ sample requires the photon to have 10 GeV or more of transverse energy, and to be in the central region. Using an event selection optimized for the $t\gamma$ candidate sample we measure the production cross section of $tt$ ($\sigma_{tt}$), and the ratio of cross sections of the two samples. Control samples in the dilepton+photon and lepton+photon+$E_T$, channels are constructed to aid in decay product identification and background measurements. We observe 30 $t\gamma$ candidate events compared to the standard model expectation of 26.9 ± 3.4 events. We measure the $t\gamma$ cross section ($\sigma_{tt\gamma}$) to be 0.18 ± 0.08 pb, and the ratio of $\sigma_{tt\gamma}$ to $\sigma_t$ to be 0.024 ± 0.009. Assuming no $t\gamma$ production, we observe a probability of 0.0015 of the background events alone producing 30 events or more, corresponding to 3.0 standard deviations.

PACS numbers: 13.85.Rm, 12.60.Jv, 13.85.Qk, 14.80.Ly

The standard model (SM) [1] of particle physics makes successful predictions of the production rates of physics processes that span many orders of magnitude. Data...
from $p\bar{p}$ collisions collected at the Tevatron have been used to verify many of these predictions [2]. As a test of the SM, we measure the ratio of production cross sections of $tt\gamma$ to $t\bar{t}$. The ratio allows for the cancellation of systematic effects, and is a more sensitive test of the SM than the measurement of the production cross section of $tt\gamma$ alone. While current data is not sufficient to study them in detail, the $tt\gamma$ coupling parameters are sensitive to some new physics models [3], and will be better measured in the future.

Top quarks are dominantly produced in pairs, with both top quarks decaying to a W boson and a b quark nearly 100% of the time. Their decays are classified as dileptonic if both W bosons decay to leptons, semileptonic if only one W boson decays to leptons, and hadronic if neither W boson decays to leptons. Selection for the $tt\gamma$ events in a semileptonic channel (including $\tau$ lepton decays) was performed using 6.0 fb$^{-1}$ of integrated luminosity from $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV collected using the CDF II detector [4]. In order to isolate non-hadronic $tt\gamma$ production, we require: a high-transverse-momentum ($p_{T}$) [5] lepton ($\ell$) identified as either an electron ($e$) or a muon ($\mu$), a photon ($\gamma$), a $b$-tagged jet ($b$), missing transverse energy ($E_{T}$), large total transverse energy ($H_{T}$), and three or more jets. With these selection criteria, $tt\gamma$ dominates SM predictions [6]. Furthermore, we select top-quark pair production ($tt$) events by using nearly the same selection as $tt\gamma$, but without the photon requirement. Using similar event selection ensures that many systematic uncertainties cancel when we measure the cross section ratio of $tt\gamma$ to $t\bar{t}$.

The semileptonic cross section of $tt\gamma$ has been measured to be 0.15 ± 0.08 pb using data corresponding to an integrated luminosity of 1.9 fb$^{-1}$ [6]. Using the branching ratio of $W$ to leptons (0.324) [7], this corresponds to a production cross section of 0.34 ± 0.18 pb. The cross section of $tt$ production is well-measured at 7.70 ± 0.52 pb [8]. However a measurement of both $tt$ and $tt\gamma$ cross sections with similar event selection has not been performed.

The CDF II detector is a cylindrically symmetric magnetic spectrometer designed to study $p\bar{p}$ collisions at the Fermilab Tevatron. Here we briefly describe the components relevant for this analysis. Tracking systems are used to measure the momenta of charged particles and to assist lepton identification. A multi-layer system of silicon strip detectors [9] which identifies tracks in the $r - \phi$ and $r - z$ views [5], and the central outer tracker (COT) [10], are contained in a superconducting solenoid that generates a 1.4 T magnetic field. The COT is a 3.1 m long open-cell drift chamber capable of making up to 96 measurements of each charged particle in the pseudorapidity region $|\eta| < 1$ [5]. Sense wires are arranged in 8 alternating axial and $\pm 2^\circ$ stereo superlayers with 12 wires each. For high-momentum tracks, the COT transverse momentum resolution is $\sigma_{p_T}/p_T^2 \simeq 0.0015$ GeV$^{-1}$.

Segmented calorimeters with towers arranged in a projective geometry, each tower consisting of an electromagnetic and a hadronic compartment [11], cover the region $|\eta| < 3.6$. In this analysis we select photons and electrons from the central region, $|\eta| \lesssim 1.0$, where the central electromagnetic shower system (CES) makes profile measurements at shower maximum with finer spatial resolution than the calorimeter. Electrons are reconstructed in the central electromagnetic calorimeter (CEM) with an $E_{T}$ [5] resolution of $\sigma(E_{T})/E_{T} \simeq 13.5\%/\sqrt{E_{T}/\text{GeV}} \pm 1.7\%$. Jets are identified using the hadronic and electromagnetic calorimeter using a cone in $\eta - \phi$ space of radius $R = \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2} = 0.4$. The jet energy resolution is approximately $\sigma \simeq 0.1 \times E_{T} \text{(GeV)} + 1 \text{ GeV}$ [12] (i.e. 2.5 GeV for a 15 GeV jet).

Jets containing a hadron with a b quark (b hadrons) are identified by exploiting the long b-hadron lifetime ($\tau_b \approx 450 \mu$m). The tracks originating from the resulting displaced vertex are used by the SecVtx [13] algorithm to identify the b hadron. The algorithm works in the region $|\eta| < 2$, defined by the silicon system coverage. Jets that are identified as coming from b hadrons are said to be b-tagged.

Muons ($\mu$) are identified using the central muon (CMU), the central muon upgrade (CMP), and the central muon extension (CMX) systems [14], which cover the detector region $|\eta| < 1$.

Luminosity is measured using Čerenkov luminosity counters in the range $3.7 < |\eta| < 4.7$. The uncertainty in the luminosity has been estimated to be 6%, where 4.4% comes from the acceptance and operation of the luminosity monitor, and 4% comes from the uncertainty on the inelastic cross section of $p\bar{p}$ [15].

A three-level online event selection system (trigger) [4] selects events with a high-$p_T$ lepton in the central region. The trigger system selects electron candidates from clusters of energy in the central electromagnetic calorimeter. Electrons are distinguished from photons by requiring a COT track associated with the clusters. The muon trigger requires a COT track that extrapolates to a track segment (“stub”) in the muon detectors.

A muon candidate passing our selection criteria must have: a well-measured track in the COT, energy deposited in the calorimeter consistent with minimum ionization expectations, a muon stub in both the CMU and CMP, or in the CMX, consistent with the extrapolated COT track, and COT timing consistent with a track from a $p\bar{p}$ collision.

An electron candidate passing our selection criteria must have: a high-quality track with $p_T > 0.5$ $E_T$, unless $E_T > 100$ GeV, in which case the $p_T$ threshold is set to 25 GeV, a good transverse shower profile that matches the extrapolated track position, a lateral sharing of energy in the two calorimeter towers containing the electron shower consistent with that expected for an electromagnetic (EM) shower, and minimal leakage into the hadron calorimeter [16].
in both transverse dimensions at shower maximum, and minimal leakage into the hadron calorimeter [16]. The detected tracks have a minimum $p_T$ of 0.35 GeV due to the magnetic field curling up lower $p_T$ particles. The photons are only reconstructed in the CEM and have $|\eta| < 1.0$.

To reduce background from photons or leptons that originate from decays of hadrons produced in jets, both the photon and the lepton in each event are required to be “isolated”. The $E_T$ deposited in the calorimeter towers in a cone in $\eta - \varphi$ space [5] of $R = 0.4$ around the photon or lepton position is summed, and the $E_T$ due to the photon or lepton is subtracted. The remaining $E_T$ is required to be less than 2.0 GeV + 0.02 × ($E_T$ - 20 GeV) for a photon, or less than 10% of the $E_T$ for electrons or $p_T$ for muons. In addition, for photons, the sum of the $p_T$ of all tracks in the cone must be less than 2.0 GeV + 0.005×$E_T$.

Missing transverse energy, $E_T$, is calculated from the observed calorimeter-tower energies in the region $|\eta| < 3.6$ [17]. Corrections are then made to the $E_T$ for non-uniform calorimeter response [18] for jets with uncorrected $E_T$ > 15 GeV and $\eta < 2$, and for muons with $p_T$ > 20 GeV.

Events for the analysis are selected by requiring a central $e$ or $\mu$ with $E_T^j > 20$ GeV originating less than 60 cm along the beam-line from the detector center and passing the criteria listed above. We further require events to have at least one of the following objects: a jet with $E_T^{jet} > 15$ GeV, $E_T > 20$ GeV, an additional lepton, or a central $\gamma$ with $E_T > 10$ GeV.

The first measurement we perform is in the $t\bar{t}$ signal sample, which requires an event to contain: $E_T > 20$ GeV, a lepton, a b-tagged jet, $H_T > 200$ GeV, $N_{jets} \geq 3$ [19] (including the b-tagged jet), and transverse mass of the lepton and $E_T$ to be greater than 20 GeV for the electron channel, and 10 GeV for the muon channel. Transverse mass for the $E_T$ and lepton is defined as:

$$\sqrt{2(E_{T,y}E_T - E_{T,x}E_{Tx} - E_{T,y}E_{Ty})}.$$

The selection criteria is inclusive, so if an event contains an additional lepton or a photon it is also accepted as a signal event. The highest-$p_T$ lepton determines if the event is an electron or muon event.

Events in the $t\bar{t}\gamma$ signal sample are selected by requiring $E_T > 20$ GeV, a lepton, a b-tagged jet, $H_T > 200$ GeV, $N_{jets} \geq 3$ (including the b-tagged jet), and a photon with $E_T > 10$ GeV. For all photons we require the $\chi^2$ of the CES shower profile be less than 20. To further suppress backgrounds, photons with $E_T$ between 10 and 25 GeV must have a $\chi^2$ of the CES shower profile less than 6; we discuss how $\chi^2$ is calculated below. Similar to the $t\bar{t}$ analysis, the selection is inclusive. The selection criteria are identical to the previous $t\bar{t}\gamma$ cross section measurement [6], with the exception of the low-$E_T$ photon $\chi^2$ requirements.

The primary difference between the $t\bar{t}$ and $t\bar{t}\gamma$ selection, other than the photon selection, is the requirement of a transverse mass selection for $t\bar{t}$. In the $t\bar{t}$ selection, the low-transverse-mass region is not well-modeled with background estimation methods. The $t\bar{t}\gamma$ sample does not suffer from this deficiency, and we do not use the transverse mass selection criterion to keep acceptance of signal events high; this behavior is also seen in the $\ell\gamma$ $E_T$ control sample described below.

Control samples are identified by selecting events with a lepton, a photon, and $E_T > 20$ GeV ($\ell\gamma E_T$), or two oppositely charged same-flavor central leptons, a photon, and a three-body mass consistent with the $Z$ boson ($t\bar{t}\gamma$). These control samples are used to define the above CES $\chi^2$ selection for photons.

The $\chi^2$ value of photons is based on the lateral shower shapes observed in the CES compared to that predicted from a sample of test-beam electrons. Using the control samples we identify an additional selection criterion on photons [20]. It should be noted that the $t\bar{t}\gamma$ sample contains 30 events and is a subset of the 8276 events in the $\ell\gamma E_T$ sample. The $\ell\gamma$ sample contains 1344 events. While the samples are not independent, optimizing photon identification selection criteria using the $t\bar{t}\gamma E_T$ sample should be minimally affected by the presence of $t\bar{t}\gamma$ events.

The dominant SM sources of events with a lepton, photon, and significant $E_T$, not including particle misidentifications, are $t\bar{t}\gamma$ production and $W\gamma$+heavy flavor (HF), in which a $W$ boson decays leptonically ($\ell\nu$) and a photon is radiated from an initial-state or final-state quark, the $W$ boson, or a charged final-state lepton [21]. In this paper, HF includes: $c\bar{c}$, $b\bar{b}$, and $c$. Similarly, for events in the $t\bar{t}$ selection, the dominant source of events is due to $t\bar{t}$ production and $W$+HF production.

The production of $t\bar{t}\gamma$ events with semileptonic and dileptonic decays, as well as the SM background of single-top events and associated production of a $W\gamma$+HF is estimated from leading-order (LO) matrix-element Monte Carlo simulations (MC) event generator MADGRAPH [22]. Events for all production and decays of $t\bar{t}$, WW, WZ, and ZZ signals are generated with PYTHIA [23]. The production of $W$+HF, as well as $Z+b\bar{b}$, and $Z \rightarrow \tau\tau$ decays are generated with ALPGEN [24]. Then the events are processed with the same reconstruction and analysis codes used for the data. Backgrounds from ZZ are estimated to be negligible to the $t\bar{t}\gamma$ signature.

Initial state radiation is simulated by the PYTHIA shower Monte Carlo simulation code tuned so as to reproduce the underlying event [25]. All of the generated samples are then passed through a full simulation of the detector, then reconstructed with the same reconstruction code used for the data.

The expected contributions from $t\bar{t}$, $W$+HF, single-top, $Z + b\bar{b}$, and $Z \rightarrow \tau\tau$ production to the $t\bar{t}\gamma$ search are given in Table I, and the expected contributions from $t\bar{t}\gamma$ and $W\gamma$+HF production to the $t\bar{t}\gamma$ search are given in Table II. Additional contributions from misidentification backgrounds, described below, are also shown in the Ta-
FIG. 1. The distributions for events in the $t\bar{t}$ sample (points) of a) the $E_T$ of the lepton; b) the missing transverse energy, $E_T$; c) the $E_T$ of the $b$ jet; and d) the total transverse energy $H_T$. The histograms show the expected SM contributions from top production ($t\bar{t}$), and miscellaneous backgrounds (Misc), which include: diboson production, single top, $W+HF$ and $Z+HF$ production as well as jets misidentified as leptons (QCD), and misidentified $b$ tags.

FIG. 2. The distributions for events in the $t\bar{t}\gamma$ sample (points) in a) the $E_T$ of the lepton; b) the missing transverse energy, $E_T$; c) the $E_T$ of the $b$ jet; and d) the $E_T$ of the photon. The histograms show the expected SM contributions from radiative top production ($t\bar{t}\gamma$), $W\gamma$ production with heavy flavor (HF), and miscellaneous backgrounds (Misc), which include: WW and WZ production as well as jets, $\tau$ leptons, electrons, and jets misidentified as photons, jets misidentified as leptons (QCD), and misidentified $b$ tags.

TABLE I. Summary for predicted and observed events in the $t\bar{t}$ ($t\bar{t}E_T^b + H_T > 200$ GeV + $N_{jets} \geq 3$) signal sample. We show the data and standard-model predictions. We show the data and standard-model predictions. We show the data and standard-model predictions.

<table>
<thead>
<tr>
<th>SM Source</th>
<th>$c\bar{b}E_T$</th>
<th>$\mu\bar{b}E_T$</th>
<th>$(e+\mu)bE_T$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t\bar{t}$</td>
<td>$1420 \pm 180$</td>
<td>$1080 \pm 140$</td>
<td>$2500 \pm 330$</td>
</tr>
<tr>
<td>WW</td>
<td>$29 \pm 4$</td>
<td>$22 \pm 3$</td>
<td>$51 \pm 7$</td>
</tr>
<tr>
<td>WZ</td>
<td>$8.6 \pm 1.1$</td>
<td>$6.5 \pm 0.9$</td>
<td>$15.1 \pm 2.0$</td>
</tr>
<tr>
<td>ZZ</td>
<td>$1.3 \pm 0.2$</td>
<td>$1.0 \pm 0.1$</td>
<td>$2.3 \pm 0.3$</td>
</tr>
<tr>
<td>Wbb</td>
<td>$203 \pm 34$</td>
<td>$146 \pm 24$</td>
<td>$348 \pm 58$</td>
</tr>
<tr>
<td>Wcc</td>
<td>$127 \pm 23$</td>
<td>$94 \pm 17$</td>
<td>$221 \pm 40$</td>
</tr>
<tr>
<td>Wc</td>
<td>$85 \pm 13$</td>
<td>$61 \pm 9$</td>
<td>$147 \pm 23$</td>
</tr>
<tr>
<td>Single top (s-ch.)</td>
<td>$76 \pm 10$</td>
<td>$59 \pm 8$</td>
<td>$135 \pm 18$</td>
</tr>
<tr>
<td>Single top (t-ch.)</td>
<td>$66 \pm 9$</td>
<td>$50 \pm 7$</td>
<td>$116 \pm 16$</td>
</tr>
<tr>
<td>$(Z\to \ell\ell)bb$</td>
<td>$31 \pm 3$</td>
<td>$22 \pm 2$</td>
<td>$53 \pm 5$</td>
</tr>
<tr>
<td>$Z \to \tau\tau$</td>
<td>$6 \pm 8$</td>
<td>$9 \pm 8$</td>
<td>$14 \pm 11$</td>
</tr>
<tr>
<td>Mistags</td>
<td>$358 \pm 29$</td>
<td>$214 \pm 17$</td>
<td>$572 \pm 46$</td>
</tr>
<tr>
<td>QCD</td>
<td>$222 \pm 38$</td>
<td>$20 \pm 3$</td>
<td>$240 \pm 40$</td>
</tr>
<tr>
<td>Total Predicted</td>
<td>$2630 \pm 196$</td>
<td>$1790 \pm 146$</td>
<td>$4420 \pm 340$</td>
</tr>
</tbody>
</table>

Observed: 2720, 1709, 4429

TABLE II. Summary for $t\bar{t}\gamma$ ($t\bar{t}E_T^b + H_T > 200$ GeV + $N_{jets} \geq 3$) Monte Carlo samples listed in the table are given as they were generated (e.g., WW was not generated with an associated photon.) Backgrounds from ZZ are found to be negligible.

<table>
<thead>
<tr>
<th>SM Source</th>
<th>$c\bar{b}E_T$</th>
<th>$\mu\bar{b}E_T$</th>
<th>$(e+\mu)\gamma bE_T$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t\bar{t}\gamma$(semilep)</td>
<td>$5.98 \pm 1.10$</td>
<td>$5.21 \pm 0.97$</td>
<td>$11.19 \pm 2.04$</td>
</tr>
<tr>
<td>$t\bar{t}\gamma$(dilep.)</td>
<td>$1.47 \pm 0.27$</td>
<td>$1.27 \pm 0.24$</td>
<td>$2.74 \pm 0.50$</td>
</tr>
<tr>
<td>WC$\gamma$</td>
<td>$0^{+0.07}_{-0.05}$</td>
<td>$0^{+0.07}_{-0.06}$</td>
<td>$0^{+0.09}_{-0.11}$</td>
</tr>
<tr>
<td>WCC$\gamma$</td>
<td>$0^{+0.05}_{-0.04}$</td>
<td>$0.05 \pm 0.07$</td>
<td>$0.21 \pm 0.08$</td>
</tr>
<tr>
<td>W$b\gamma$</td>
<td>$0.15 \pm 0.07$</td>
<td>$0.06 \pm 0.05$</td>
<td>$0.09 \pm 0.06$</td>
</tr>
<tr>
<td>W$Z\gamma$</td>
<td>$0.05 \pm 0.05$</td>
<td>$0.06 \pm 0.05$</td>
<td>$0.11 \pm 0.03$</td>
</tr>
<tr>
<td>WW</td>
<td>$0.06 \pm 0.03$</td>
<td>$0.06 \pm 0.03$</td>
<td>$0.11 \pm 0.03$</td>
</tr>
<tr>
<td>Single Top (s-chan)</td>
<td>$0.09 \pm 0.10$</td>
<td>$0 \pm 0.10$</td>
<td>$0.09 \pm 0.13$</td>
</tr>
<tr>
<td>Single Top (t-chan)</td>
<td>$0.14 \pm 0.14$</td>
<td>$0.13 \pm 0.14$</td>
<td>$0.27 \pm 0.19$</td>
</tr>
<tr>
<td>$\tau \to \gamma$ fake</td>
<td>$0.20 \pm 0.08$</td>
<td>$0.10 \pm 0.05$</td>
<td>$0.29 \pm 0.09$</td>
</tr>
<tr>
<td>Jet faking $\gamma$</td>
<td>$5.75 \pm 1.76$</td>
<td>$1.79 \pm 1.56$</td>
<td>$7.54 \pm 2.53$</td>
</tr>
<tr>
<td>Mistags</td>
<td>$1.47 \pm 0.37$</td>
<td>$1.02 \pm 0.32$</td>
<td>$2.50 \pm 0.51$</td>
</tr>
<tr>
<td>QCD</td>
<td>$0.38 \pm 0.38$</td>
<td>$0.02 \pm 0.02$</td>
<td>$0.40 \pm 0.38$</td>
</tr>
<tr>
<td>$eeE_T^b, e\to \gamma$</td>
<td>$0.94 \pm 0.19$</td>
<td>$-0.49 \pm 0.11$</td>
<td>$0.49 \pm 0.11$</td>
</tr>
</tbody>
</table>

Total Predicted: 16.7 $\pm$ 2.2, 10.3 $\pm$ 1.9, 26.9 $\pm$ 3.4

Observed: 17, 13, 30
as a photon (jet faking photon) is estimated by removing the isolation requirements on the photon. We fit the resulting isolation distribution using signal and background templates obtained from data. The signal template is constructed using electrons from $Z\gamma \rightarrow e e$ events, and a background template is made from a QCD enriched sample [20, 26].

The expected number of events in which an electron is misidentified as a photon in the $t\bar{t}\gamma$ signature is determined by measuring the electron $E_T$ spectrum in the $t\bar{t}$ signature; each jet in the $t\bar{t}$ signature is created from dileptonic, $ee$ or $e\mu$, $t\bar{t}$ and di-boson decays), and then multiplying by the probability that an electron is misidentified as a photon. The latter is measured in data using $Z\gamma \rightarrow e e$ events that are misreconstructed as $Z\gamma \rightarrow e \gamma$.

To estimate the number of $b$-tagged jets that are in reality mistagged light-quark jets (mistags), each jet in the $t\bar{t}+\gamma$ sample is weighted by a mistag rate. The mistag rate per jet is measured using a large inclusive-jet sample. For the $t\bar{t}$ sample, a similar procedure is used. Each jet in the signal samples has a corresponding probability to be identified as a $b$-tagged jet. In all cases, however, the resulting prediction is overestimated because we count as mistags, events which have true heavy flavor jets (i.e., events due to $t\bar{t}$ events may be mistagged, but they will be accounted for in the MC). The fraction of events that have no true heavy flavor content relative to the size of dileptonic or $t\bar{t}$ analogue sample is used to scale our mistag estimate. This scaled background estimate removes events which contain actual heavy flavor content from the mistag total; the scale factor is nearly 60%.

The background due to events in which a jet is misidentified as a lepton (QCD) is estimated using “non-electrons”. “Non-electrons” are jets which are kinematically similar to electrons, but which fail a pair of selection criteria normally passed by electrons (regardless of energy) such as: EM shower-shape, energy over momentum, or isolation. “Non-electrons” play the role of leptons in our model of the QCD background. The remaining object selection is unchanged. In each signature, a template of signal events in data with $E_T < 20$ GeV are fit to the sum of MC backgrounds and a scaled “non-electron” signal. The QCD background is the sum of the scaled “non-electron” events in the $E_T > 20$ GeV region expected from the fit.

To avoid double counting, the total background yields are corrected by removing the predicted number of events with two objects misidentified. Each of the aforementioned data-driven background estimates accounts for a background process where one object in the event is misidentified. Events with two misidentified objects would be counted in a pair of background estimates. In the $t\bar{t}$ sample, double counting is accounted for by removing the QCD background from the mistagging background, and vice versa.

The background from tau leptons, which decay to hadrons, which decay to photons is a background estimated from the $t\bar{t}$ MC sample by selecting $\tau \rightarrow hadrons \rightarrow \gamma$ events using MC information.

The $t\bar{t}$ event detection efficiency and acceptance are calculated using the MC simulation which has all decays of $t\bar{t}$. The uncertainty on the $t\bar{t}$ cross section is dominated by systematic uncertainties. The $t\bar{t}$ event detection efficiency and acceptance are calculated using both semileptonic, and dileptonic decays of the pair of top quarks in the decay. The total $t\bar{t}$ cross section is then calculated assuming that $t\bar{t}$ has the same branching ratio to semileptonic and dileptonic decays as $t\bar{t}$ pair production.

The uncertainty in the $t\bar{t}$ cross section measurement is dominated by statistics.

Systematic uncertainties have been calculated by varying detector efficiencies and resolutions within known uncertainties and evaluating the change in our measurements. These uncertainties are added in quadrature when independent, and summed when positively (or negatively) correlated. The largest uncertainties, given in descending order, are due to luminosity, $b$-hadron tagging efficiencies and, for the $t\bar{t}\gamma$ sample, photon identification.

We observe 30 $t\bar{t}\gamma$ candidate events compared to an expectation of $26.9 \pm 3.4$. We observe 4429 $t\bar{t}$ events, with an expectation of $4420 \pm 340$. Assuming the difference between the non-$t\bar{t}$ background estimate and the number of observed events is due to SM $t\bar{t}$ production, we measure the $t\bar{t}$ cross section to be $7.62 \pm 0.20$ (stat) $\pm 0.68$ (sys) $\pm 0.46$ (lum) pb. The theoretical production cross section of $t\bar{t}$ at the Tevatron is $7.08_{-0.32}^{+0.36}$ pb [27].

If one assumes that $t\bar{t}\gamma$ is not allowed in the SM, and there are no new physics processes contributing to this sample, the probability that the background events alone will produce 30 or more events is 0.0015 (3.0 standard deviations). This is the first experimental evidence for $t\bar{t}\gamma$ production. Assuming the difference between the background estimate and the number of observed events is due to SM $t\bar{t}\gamma$ production, we measure the $t\bar{t}\gamma$ cross sec-

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**FIG. 3.** The distributions for events in the $t\bar{t}\gamma$ sample (points) of a) the total transverse energy $H_T$, the sum of the transverse energies of the lepton, photon, jets and $E_T$ for the $t\bar{t}\gamma$ events; b) the total number of jets. The histograms show the expected SM contributions from radiative top-quark pair production ($t\bar{t}\gamma$), $W\gamma$ production with heavy flavor ($W\gamma+HF$), and miscellaneous backgrounds (Misc), which include: SM $WW$ and $WZ$ production as well as jets, $\tau$ leptons, electrons, and jets misidentified as photons, jets misidentified as leptons (QCD), and misidentified $b$ tags.
tion to be 0.18±0.07 (stat) ±0.04 (sys) ±0.01 (lum) pb. The \( t\bar{t}\gamma \) event detection efficiency and acceptance are calculated using the MC sample requiring at least one W boson decaying leptonically. The acceptance times efficiency, using both semi-leptonic and dileptonic modes, for this \( t\bar{t}\gamma \) signal is 0.015 ± 0.002. The uncertainty on the measured cross section is dominated by the statistical uncertainties associated with the small number of events observed. A theoretical value for the non-hadronic decays of \( t\bar{t}\gamma \) (sum of all three lepton flavors) cross section \( \sigma_{t\bar{t}\gamma} = 0.071 \pm 0.011 \) pb is obtained from leading order (LO) MadGRAPH semileptonic cross section \( \sigma_{t\bar{t}\gamma} = 0.0726 \) pb multiplied by a K-factor to find the next to leading order (NLO); K-factor = \( \sigma_{NLO}/\sigma_{LO} = 0.977 \). The next to leading order theoretical total cross section for \( t\bar{t}\gamma \) is then \( \sigma_{t\bar{t}\gamma}^\text{total} = 0.17 \pm 0.03 \) pb.

The ratio between the production cross sections of \( t\bar{t}\gamma \) and \( t\bar{t} \) is measured to be \( R = 0.024 \pm 0.009 \) which agrees with the SM prediction of \( R = 0.024 \pm 005 \), obtained from theoretical predictions of the cross sections of \( t\bar{t}\gamma \) and \( t\bar{t} \). When measuring \( R \) many of the systematic uncertainties nearly cancel, such as those due to: lepton identification, hadron identification, jet energy scale, and luminosity uncertainties. However, other systematic uncertainties do not cancel out completely such as: QCD systematic uncertainties, and photon identification and acceptance uncertainties. The total systematic uncertainties combine to less than 10% however the statistical uncertainty is the dominant contribution to the total uncertainty.

In conclusion, we have performed a search for \( t\bar{t}\gamma \), which is the dominant standard model process that produces the event signature of lepton + photon + \( E_T \) + b-jets with large total transverse energy and \( N_{\text{jets}} \geq 3 \). We find that the numbers of events observed are consistent with SM predictions. We obtain a \( t\bar{t}\gamma \) cross section \( \sigma_{t\bar{t}\gamma} = 0.18 \pm 0.08 \) pb, and the ratio of production cross sections of \( t\bar{t}\gamma \) to \( t\bar{t} \) is \( 0.024 \pm 0.009 \).

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[5] The CDF coordinate system of \( r, \phi, \) and \( z \) is cylindrical, with the \( z \)-axis along the proton beam. The pseudorapidity is \( \eta = -\ln(\tan(\theta/2)) \). Transverse momentum and energy are defined as \( p_T = p \sin \theta \) and \( E_T = E \sin \theta \), respectively. We use the convention that “momentum” refers to \( p \) and “mass” to \( m c^2 \). The coordinate \( y \) points up and down, and \( x \) completes the right-handed system.
[14] The CMU consists of a central barrel of gas proportional wire chambers in the region \( |\eta| < 0.6 \); the CMP system consists of chambers after an additional meter of steel, also for \( |\eta| < 0.6 \). The CMX chambers cover 0.6 < \( |\eta| < 1.0 \).
[16] The fraction of electromagnetic energy allowed to leak into the hadron compartment \( E_{\text{had}}/E_{\text{em}} \) must be less than 0.055 + 0.00045 \times E_{\text{em}}(\text{GeV}) \) for central electrons, less than 0.05 for electrons in the end-plug calorimeters, less than max[0.125, 0.055+0.00045 \times E_{\text{em}}(\text{GeV})] for photons.
[17] Missing \( E_T \) (\( \vec{E}_T \)) is defined by \( \vec{E}_T = - \sum_i E_i \hat{n}_i \), where \( i \) is the calorimeter tower number for \(|\eta| < 3.6\), and \( \hat{n}_i \) is a unit vector perpendicular to the beam axis and pointing at the \( i^{th} \) tower. We correct \( \vec{E}_T \) for jets and muons. We define the magnitude \( E_T = |\vec{E}_T| \).